

621.

ON THE NUMBER OF THE UNIVALENT RADICALS C_nH_{2n+1} .

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I HAVE just remarked that the determination is contained in my paper "On the Analytical Forms called Trees, &c.," *British Association Report*, 1875, [610]; in fact, in the form C_nH_{2n+1} , there is one carbon atom distinguished from the others by its being combined with (instead of 4, only) 3 other atoms; viz. these are 3 carbon atoms, 2 carbon atoms and 1 hydrogen atom, or else 1 carbon atom and 2 hydrogen atoms (CH_3 , methyl, is an exception; but here the number is =1). The number of carbon atoms thus combined with the first-mentioned atom is the number of main branches, which is thus = 3, 2, or 1; hence we have, number of radicals C_nH_{2n+1} is =

No. of carbon root-trees C_n with one main branch,
 + No. of " " with two main branches,
 + No. of " " with three main branches;

and the three terms for the values $n=1$ to 13 are given in Table VII. (pp. 454, 455 of this volume) of the paper referred to.

Thus, if $n=5$, an extract from the Table (p. 454 of this volume), is

Index x , or number of knots	Index t , or number of main branches	Altitude					
		0	1	2	3	4	
5	1			1	2	1	4
	2			2	1		3
	3			1			1
	4		1				1
	Total ...		1	4	3	1	9

and the number of the radicals C_5H_{11} (isomeric amyls) is $4 + 3 + 1 = 8$: or, what is the same thing, it is $9 - 1$, the corner-total less the number immediately above it. The tree-forms corresponding to the numbers 1, 2, 1; 2, 1; 1 in the body of the Table are the trees 2 to 9 in the figure, p. 428 of this volume.

The numbers of the radicals C_nH_{2n+1} , as obtained from the Table in the manner just explained, are:—

$n =$	Number of radicals C_nH_{2n+1} .		
1	1	=	1 Methyl.
2	1		1 Ethyl.
3	1		1 Propyl.
4	4		4 Butyls.
5	9 - 1		8 Amyls.
6	18 - 1		17 Hexyls.
7	42 - 3		39 Heptyls.
8	96 - 7		89 Octyls.
9	229 - 18		211 Nonyls.
10	549 - 42		507 Decyls.
11	1346 - 108		1238 Undecyls.
12	3326 - 269		3057 Dodecyls.
13	8329 - 691		7638 Tridecyls.

The question next in order, that of the determination of the number of the bivalent radicals C_nH_{2n} , might be solved without much difficulty.

Cambridge, November 20, 1876.