

## MERSENNE'S NUMBERS.

(Addition to a previous paper, pp. 34-36).

By *W. W. Rouse Ball.*

IN the paper on Mersenne's Numbers which appears in the current volume of the *Messenger* (pp 34-40) I stated (Art. 10) that I believed that the factors of  $2^p - 1$  when  $p=29$  were discovered by Euler, but that I had mislaid my reference and could not quote an earlier authority than Plana. I am able now to supply the reference. The memoir by Euler which contains the result was written in 1732 and appears in the *Comment. Petropol.*, Vol. VI., p. 103; or the *Commentationes Arithmeticae Collectae*, Vol. I., p. 2.

This memoir contains also the factors of  $2^p - 1$  when  $p=43$  and when  $p=73$ ; of which results I attributed (Arts. 12, 14) the first enunciation to MM. Landry and Le Lasseur respectively.

The theorem which I attributed (Art. 11) to M. Lucas was enunciated by Euler in the same memoir: hence the credit of the discovery of the factors of  $2^p - 1$  for the values  $p=83, 131, 179, 191, 239, 251, \dots$  should be assigned to Euler.

Lastly I regret to say that in consequence of my having used an old and inaccurate table of powers of 2 there are a few mistakes. In the table on p. 35, the value of  $2^p - 1$  when  $p=67$  should be 14757... instead of 13957...; the value when  $p=71$  should be 236118... instead of 223318...; the value when  $p=89$  should be ...196426901374... instead of 195176901874...; the value when  $p=101$  should be ...458802993... instead of ...459007793...; and the value when  $p=127$  should be ...4604692...68...105... instead of ...3324884...04...361.... In article 20 the ninth perfect number should be 2658455991569831744654692615953842176.